MATH 320, Spring 2013, Assignment 3 Textbook Questions

Section 1.6 Find the general solution of the following differential equations:

#10
$$xyy' = x^2 + 3y^2$$

#15 $x(x+y)y' + y(3x+y) = 0$
#23 $xy' + 6y = 3xy^{4/3}$
#24 $2xy' + y^3e^{-2x} = 2xy$

Verify that the given differential equation is exact, then solve it:

#35
$$\left(x^3 + \frac{y}{x}\right) dx + (y^2 + \ln(x)) dy = 0$$

#38 $(x + \arctan(y)) dx + \left(\frac{x+y}{1+y^2}\right) dy = 0$

#56 Suppose that $n \neq 0$ and $n \neq 1$. Show that the substitution $v = y^{1-n}$ transforms the Bernoulli equation $dy/dx + P(x)y = Q(x)y^n$ into the linear equation

$$\frac{dv}{dx} + (1-n)P(x)v(x) = (1-n)Q(x).$$